

# ELLIPTICAL ORBIT

Radius, speed, gravitational force, energy, and angular momentum

|             |               |             |
|-------------|---------------|-------------|
| Name: _____ | Period: _____ | Date: _____ |
|-------------|---------------|-------------|

## INVESTIGATION QUESTION How do orbital speed and gravitational force change between apoapsis and periapsis?

|                    |                                               |                                                 |
|--------------------|-----------------------------------------------|-------------------------------------------------|
| TIME<br>30 minutes | SIMULATION<br>BuildPhysics > Elliptical orbit | UNIT 6<br>Energy & Momentum of Rotating Systems |
|--------------------|-----------------------------------------------|-------------------------------------------------|

### Learning targets

- Compare orbital quantities at apoapsis and periapsis.
- Test conservation of angular momentum in a central-force orbit.
- Track kinetic, gravitational potential, and total mechanical energy.

### Model before you measure

|                                                                                                                                              |                                                                             |
|----------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------|
| Gravity is a central force, so its torque about the planet center is zero. The satellite moves fastest at periapsis and slowest at apoapsis. | $L = mrv_t = \text{constant}$ $E = \frac{1}{2}mv^2 - GMm/r$ $F_g = GMm/r^2$ |
| <b>Important:</b> Use the planet center as the angular-momentum axis. Record radius from the planet center to the satellite center.          |                                                                             |

### Pre-lab prediction | 4 minutes

1. At which point should speed be greatest: apoapsis or periapsis?  
\_\_\_\_\_
2. At which point should gravitational-force magnitude be greatest?  
\_\_\_\_\_
3. Predict how total mechanical energy changes during one complete orbit.  
\_\_\_\_\_

## PART A Analyze one complete elliptical orbit

### Setup | 3 minutes

- ☐ Load Elliptical orbit. Turn on the trail and graph radius, speed, gravitational force, kinetic energy, and gravitational potential energy.
- ☐ Run at least one complete orbit and identify apoapsis and periapsis from the radius graph.
- ☐ Pause at apoapsis and periapsis and record all requested quantities.
- ☐ Calculate  $mr\mathbf{v}$  at each point using the tangential speed.

### Apoapsis-periapsis data | 10 minutes

| Location  | Radius $r$<br>(m) | Speed $v$<br>(m/s) | $ F_g $<br>(N) | $K$<br>(J) | $U_g$<br>(J) | Angular momentum<br>$mr\mathbf{v}$<br>( $\text{kg}\cdot\text{m}^2/\text{s}$ ) |
|-----------|-------------------|--------------------|----------------|------------|--------------|-------------------------------------------------------------------------------|
| Apoapsis  |                   |                    |                |            |              |                                                                               |
| Periapsis |                   |                    |                |            |              |                                                                               |

### Energy comparison | 3 minutes

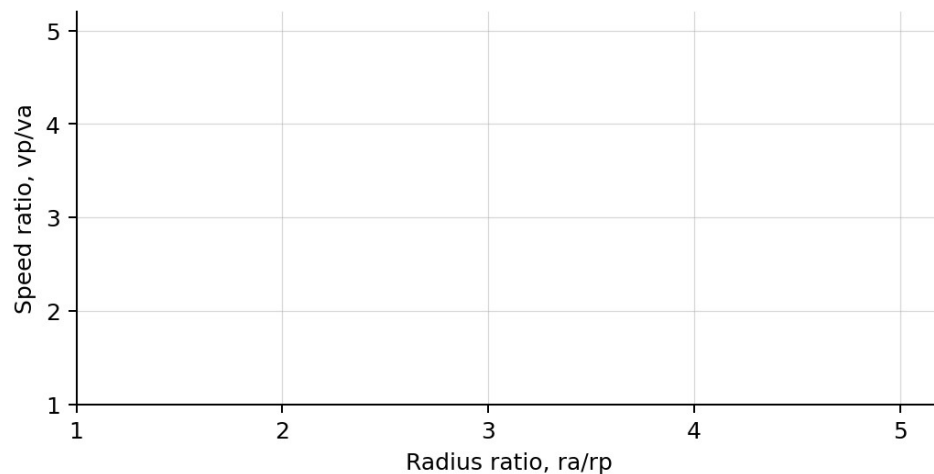
| Total mechanical energy at apoapsis<br>(J) | Total mechanical energy at periapsis<br>(J) | Orbital period<br>(s) |
|--------------------------------------------|---------------------------------------------|-----------------------|
|                                            |                                             |                       |

## PART B Change the initial tangential speed

### Orbit-shape test | 8 minutes

**Procedure:** Reset to the same starting radius. Change only the initial tangential speed, run one orbit, and record the new apoapsis and periapsis values.

| Trial   | Initial speed (m/s) | $r_a / r_p$ | $v_p / v_a$ | Total mechanical energy (J) | Orbit classification |
|---------|---------------------|-------------|-------------|-----------------------------|----------------------|
| Trial 1 |                     |             |             |                             |                      |
| Trial 2 |                     |             |             |                             |                      |
| Trial 3 |                     |             |             |                             |                      |
| Trial 4 |                     |             |             |                             |                      |



4. Plot speed ratio  $v_p/v_a$  versus radius ratio  $r_a/r_p$ . Draw a best-fit line.

### Analysis | 6 minutes

5. Compare angular momentum at apoapsis and periapsis.

6. How did kinetic and gravitational potential energy trade off during the orbit?

7. Why should  $v_p/v_a$  equal  $r_a/r_p$  at the two apsides?

8. How did changing initial speed affect orbit shape and total mechanical energy?

### Claim-Evidence-Reasoning conclusion

**Evaluate this claim:** The satellite moves faster at periapsis because gravity does more positive work there than at other parts of the orbit.

|           |                                                                                                 |
|-----------|-------------------------------------------------------------------------------------------------|
| CLAIM     | Accept, reject, or revise the statement.                                                        |
| EVIDENCE  | Cite at least two measured trials or graph features.                                            |
| REASONING | Use central-force torque, angular momentum conservation, and energy changes over the full path. |

### Exit ticket

At apoapsis the orbital radius is three times the periapsis radius. Use angular momentum conservation to predict  $v_p/v_a$ .

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